LESSON 4-3

Angle Relationships in Triangles

According to the **Triangle Sum Theorem**, the sum of the angle measures of a triangle is 180°.

 $m \angle J + m \angle K + m \angle L = 62 + 73 + 45$

= 180°

The **corollary** below follows directly from the Triangle Sum Theorem.



Date _____ Class



Use the figure for Exercises 1 and 2.

- 1. Find m∠ABC.
- 2. Find m $\angle CAD$.

Use $\triangle RST$ for Exercises 3 and 4.

3. What is the value of *x*?



84°

C

/46°

n 4

4. What is the measure of each angle?

What is the measure of each angle?









R

Reteach LESSON 4-3

Angle Relationships in Triangles continued

An **exterior angle** of a triangle is formed by one side of the triangle and the extension of an adjacent side.

 $\angle 1$ and $\angle 2$ are the remote interior angles of



 $\angle 4$ because they are not adjacent to $\angle 4$.

The measure of an exterior angle of a triangle is equal to the sum of the measures of its remote interior angles.



If two angles of one triangle are congruent to two angles of another triangle, then the third pair of angles are congruent.



Find each angle measure.





9. m∠D

Find each angle measure.



10. m $\angle M$ and m $\angle Q$





exterior angle	8. 1	15°
70°	10. 6	i0°
65°	12. 3	5°
120°	14. 1	10°
	exterior angle 70° 65° 120°	exterior angle 8. 1 70° 10. 6 65° 12. 3 120° 14. 1

Practice B

1.	101.1°	2.	45°
3.	45.1°	4.	Z°
5.	89.7°	6.	60°
7.	47°	8.	33°; 66°; 81°
9.	44°; 44°	10.	108°; 108°
11.	55°	12.	54°; 72°; 54°

Practice C



1. Possible answer:

Statements	Reasons
1. Quadrilateral ABCD	1. Given
2. Draw AC.	2. Construction
3. $m \angle D + m \angle DAC + m \angle DCA =$ 180°, $m \angle B + m \angle BAC +$ $m \angle BCA =$ 180°	3. Triangle Sum Thm.
4. $m \angle D + m \angle DAC + m \angle DCA + m \angle B + m \angle BAC + m \angle BCA = 360^{\circ}$	4. Add. Prop. of =
5. $m \angle DAC + m \angle BAC =$ $m \angle DAB$, $m \angle DCA + m \angle BCA$ $= m \angle DCB$	5. Angle Add. Post.
6. $m \angle D + m \angle DAB + m \angle B + m \angle DCB = 360^{\circ}$	6. Subst.

2.
$$\begin{array}{c} m \angle 5 = m \angle 1 + m \angle 3 \\ m \angle 6 = m \angle 1 + m \angle 2 \\ m \angle 4 = m \angle 3 + m \angle 2 \\ \hline \text{Ext. } \angle \text{ Thm.} \\ \hline m \angle 5 + m \angle 6 + m \angle 4 = \\ 2m \angle 1 + 2m \angle 2 + 2m \angle 3 \\ \hline \text{Add. Prop. of =} \\ \hline m \angle 1 + m \angle 2 + m \angle 3 = 180^{\circ} \\ \hline \ \Delta \text{ Sum Thm.} \\ \hline \end{array}$$

- 3. 360°
- 4. interior = 540° ; exterior = 360°
- 5. *x* = 93; *y* = 52; *z* = 35

Reteach

1.	47°	2.	38°
3.	14		
4.	$m \angle R = 85^\circ; m \angle S = 36$	0°; m	n∠ <i>T</i> =65°
5.	49°	6.	39.8°
7.	(90 – <i>x</i>)°	8.	51°
9.	41°	10.	82°; 82°
11.	33°; 33°		

Challenge

1. 39°	
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3. Through *C*, draw line $\ell \parallel \overline{BA}$. So ℓ is also $\parallel DE$. Then apply the Alt. Int. \angle Thm. twice, followed by the \angle Add. Post. $x^{\circ} = 55^{\circ} + 62^{\circ} = 117^{\circ}$.

2.88°



4. Additional Answer: Proofs will vary.
Given: △ABC with exterior angle △BCD
Prove: m∠BCD = m∠1 + m∠2
Proof:



Statements	Reasons
1. ∠ABC with exterior angle ∠BCD	1. Given
2. Through C, draw line ℓ parallel to <u>AB</u> .	2. Through a point outside a line, there is exactly one line parallel to the given line.
3. m∠1 = m∠3	3. lines \rightarrow corr. \measuredangle \cong
4. m∠2 = m∠4	4. lines \rightarrow alt. int. $\measuredangle \cong$
$5. m \angle BCD = m \angle 3 + m \angle 4$	5. ∠ Add. Post.
6. m∠ <i>BCD</i> = m∠1 + m∠2	6. Subst. Prop. of =

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